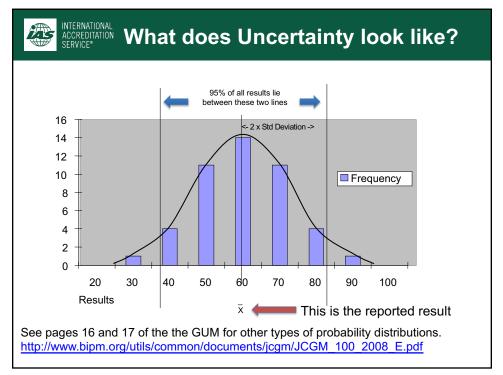
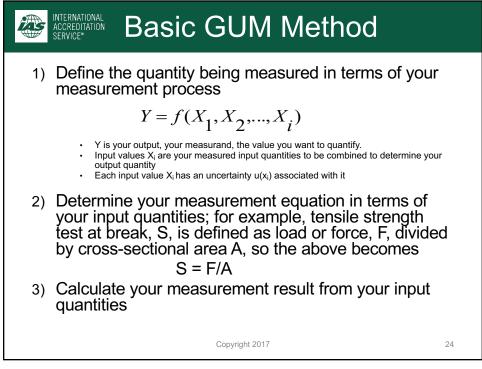
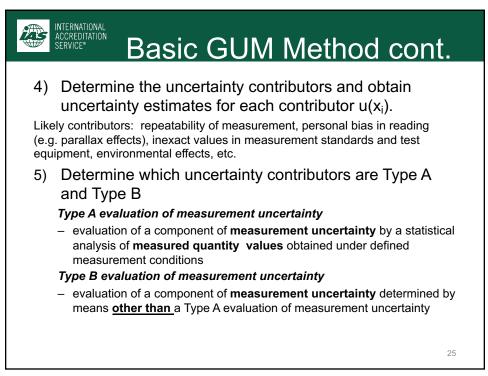
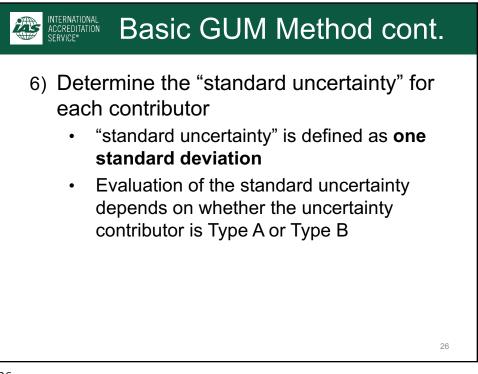


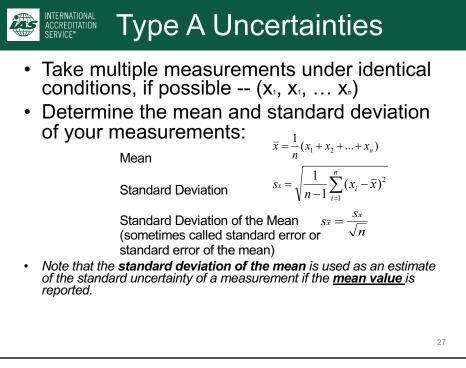
<complex-block>











Cal	culating the	e Mean and Stan	dard Deviatio	on of a Sample
Point	Dat	ta Set 1	Da	ata Set 2
No.	<i>x</i> <sub>1</sub>			
1	80			
2	81			
3	79			
4	82			
5	78			
6	79			
7	81			

Service 1	caracin	Data Set 1	nd Standard De	Data Set 2	
Point -	<i>x</i> ,	Putti Jot I	X2	Data Set 1	
1	80		80		
2	81		70		
3	79		90		
4	82 78		85		
5	78 79		75		
7	79 81		78		
-	01	the second s	78	5	

Sec. Col	realizing	the Mean and Data Set 1	Standard Be	Data Set 2	
Point - No.	$\boldsymbol{x}_{i}$		<i>X</i> <sub>2</sub>		
1	80		80		
2	81		70		
3	79		90		
4	82		85		
5	78		75		
6	79		82		
7	81		78		
Sum	560		560		

Ca	alculating			ndard Dev			npie
Point		Data Set	1		Data	Set 2	
No.	$\boldsymbol{x}_{i}$			<i>X</i> <sub>2</sub>			
1	80			80			
2	81			70			
3	79			90			
4	82			85			
5	78			75			
6	79			82			
7	81			78			
Sum	560			560			
avg (mean)	$\overline{x}_1 = \frac{560}{7} = 80$			$\overline{x_2} = \frac{560}{7} = 80$			
(mean)							

Ca	lculatin	g the Mean a	nd Standard			ple
Point		Data Set 1		Da	ata Set 2	
No.	<i>x</i> <sub>1</sub>	$\left(x-\overline{x}\right)$	x	2		
1	80	80-80=0	80	)		
2	81	81-80=1	70	)		
3	79	79-80=-1	90	)		
4	82	82-80=2	85	5		
5	78	78-80=-2	75	5		
6	79	79-80=-1	82	2		
7	81	81-80=1	78	3		
Sum	560		56	0		
avg (mean)	$\frac{-}{x_1} = \frac{560}{7} = 80$		$\overline{x_2} = \frac{56}{7}$	<sup>0</sup> = 80		

		Data S		Standard Devi	Data Set	
Point No.	<i>x</i> <sub>1</sub>	$(x-\overline{x})$	$\frac{1}{\left(x-\overline{x}\right)^2}$	<i>x</i> <sub>2</sub>	Dutu Det	
1	80	80-80=0	0	80		
2	81	81-80=1	1	70		
3	79	79-80=-1	1	90		
4	82	82-80=2	4	85		
5	78	78-80=-2	4	75		
6	79	79-80=-1	1	82		
7	81	81-80=1	1	78		
Sum	560		12	560		
avg (mean)	$\overline{x_1} = \frac{560}{7} = 80$			$\overline{x_2} = \frac{560}{7} = 80$		

Ca	lculatin	and the second s		nd Sta	ndard Dev			nple
Point		Data S		_		Data	Set 2	
No.	$\boldsymbol{x}_{i}$	$\left(x-\overline{x}\right)$	$\left(x-\overline{x}\right)^2$		$X_2$			
1	80	80-80=0	0		80			
2	81	81-80=1	1		70			
3	79	79-80=-1	1		90			
4	82	82-80=2	4		85			
5	78	78-80=-2	4		75			
6	79	79-80=-1	1		82			
7	81	81-80=1	1		78			
Sum	560		12/6 = 2	$= S_1^2$	560		8	
avg (mean)	$\overline{x}_1 = \frac{560}{7} = 80$		(Vari	ance)	$\overline{x_2} = \frac{560}{7} = 80$			
(mean)	1							

		Data S		iu Sta	ndard Dev		Set 2	inhie
Point No.	<i>x</i> <sub>1</sub>	$(x-\overline{x})$	$\left(x-\overline{x}\right)^2$		<i>X</i> <sub>2</sub>			
1	80	80-80=0	0		80			-
2	81	81-80=1	1		70			
3	79	79-80=-1	1		90			
4	82	82-80=2	4		85			
5	78	78-80=-2	4		75			
6	79	79-80=-1	1		82			
7	81	81-80=1	1		78			
Sum	560		12/6 = 2	$= S_1^2$	560			
avg (mean)	$\overline{x_1} = \frac{560}{7} = 80$		(Vari	ance)	$\overline{x_2} = \frac{560}{7} = 80$	-		

Ca	alculatin	g the M	lean ar	nd Sta	ndard Dev	iation	of a San	nple
Point		Data S	Set 1			Data	Set 2	
No.	<i>x</i> <sub>1</sub>	$\left(x-\overline{x}\right)$	$\left(x-\overline{x}\right)^2$		<i>x</i> <sub>2</sub>			
1	80	80-80=0	0		80			
2	81	81-80=1	1		70			
3	79	79-80=-1	1		90			
4	82	82-80=2	4		85			
5	78	78-80=-2	4		75			
6	79	79-80=-1	1		82			
7	81	81-80=1	1		78			
Sum	560		12/6 = 2	$= S_1^2$	560			
avg (mean)	$\overline{x}_1 = \frac{560}{7} = 80$		(Vari	ance)	$\overline{x_2} = \frac{560}{7} = 80$			
Standar	d Deviation =	$= \sqrt{(S_1)^2}$	= 1.4					

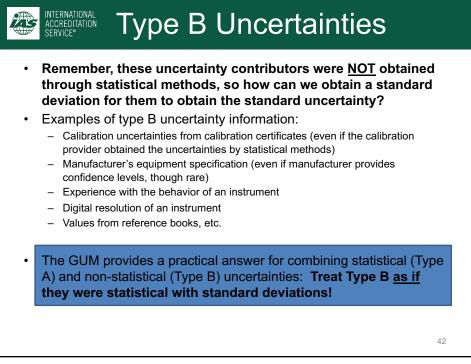
Ca	alculatin			nd Sta	ndard De			nple
Point		Data S			1	Data S	Set 2	
No.	$\boldsymbol{x}_{1}$	$\left(x-\overline{x}\right)$	$\left(x-\overline{x}\right)^2$		<i>X</i> <sub>2</sub>	$\left(x-\overline{x}\right)$		
1	80	80-80=0	0		80	80-80=0		
2	81	81-80=1	1		70	70-80=-10		
3	79	79-80=-1	1		90	90-80=10		
4	82	82-80=2	4		85	85-80=5		
5	78	78-80=-2	4		75	75-80=-5		
6	79	79-80=-1	1		82	82-80=2		
7	81	81-80=1	1		78	78-80=-2		
Sum	560		12/6 = 2	$= S_1^2$	560			
avg (mean)	$\overline{x}_1 = \frac{560}{7} = 80$		(Vari	ance)	$\overline{x_2} = \frac{560}{7} = 80$	c		
Chandan	d Deviation =	$= \sqrt{(S_1)^2}$	= 1.4			_		

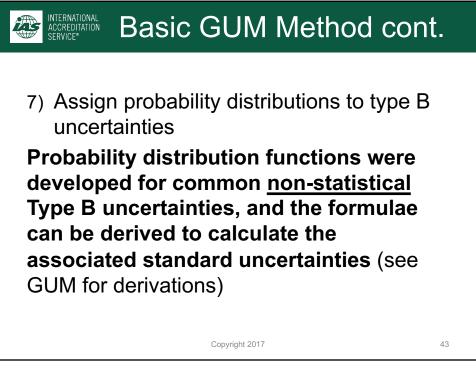
Ca	lculatin	g the M	lean ar	nd Sta	ndard De	viation	of a Sam	ple
Point		Data S				Data		
No.	<i>x</i> <sub>1</sub>	$\left(x-\overline{x}\right)$	$\left(x-\overline{x}\right)^2$		<i>X</i> <sub>2</sub>	$\left(x-\overline{x}\right)$	$\left(x-\overline{x}\right)^2$	
1	80	80-80=0	0		80	80-80=0		
2	81	81-80=1	1		70	70-80=-10		
3 4	79	79-80=-1	1		90	90-80=10		
4	82	82-80=2	4		85	85-80=5		
5	78	78-80=-2	4		75	75-80=-5		
6	79	79-80=-1	1		82	82-80=2		
7	81	81-80=1	1		78	78-80=-2		
Sum	560		12/6 = 2	$= S_1^2$	560			
avg (mean)	$\bar{x}_1 = \frac{560}{7} = 80$		(Vari	ance)	$\overline{x_2} = \frac{560}{7} = 80$		(Varia	nce)
Standar	d Deviation =	$= \sqrt{(S_i)^2}$	= 1.4			$\sqrt{(S_2)^2}$		

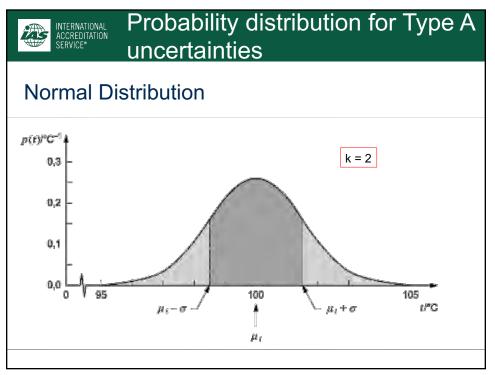
Ca	lculatin	a the M	lean ar	nd Sta	ndard De	viation	of a Sam	ple
Point		Data S				Data		
No.	<i>x</i> <sub>1</sub>	$\left(x-\overline{x}\right)$	$\left(x-\overline{x}\right)^2$		<i>X</i> <sub>2</sub>	$\left(x-\overline{x}\right)$	$\left(x-\overline{x}\right)^2$	
1	80	80-80=0	0		80	80-80=0	0	
2	81	81-80=1	1		70	70-80=-10	100	
3	79	79-80=-1	1		90	90-80=10	100	
4	82	82-80=2	4		85	85-80=5	25	
5	78	78-80=-2	4		75	75-80=-5	25	
6	79	79-80=-1	1		82	82-80=2	4	
7	81	81-80=1	1		78	78-80=-2	4	
Sum	560		12/6 = 2	$= S_1^2$	560		6.5.6	1.1
avg (mean)	$\overline{x}_1 = \frac{560}{7} = 80$		(Vari	ance)	$\overline{x_2} = \frac{560}{7} = 80$		(Varia	ince)
Standard	d Deviation =	$= \sqrt{(S_i)^2}$	= 1.4			$\sqrt{(S_2)^2}$		

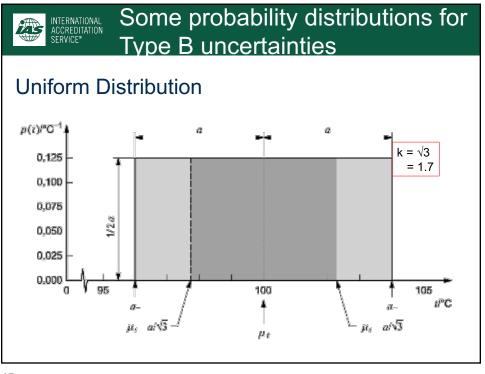
Ca	alculatin	a the M	lean ar	nd Sta	ndard De	viation	of a Sam	ple
Point		Data S					Set 2	
No.	<i>x</i> <sub>1</sub>	$\left(x-\overline{x}\right)$	$\left(x-\overline{x}\right)^2$		<i>X</i> <sub>2</sub>	$\left(x-\overline{x}\right)$	$\left(x-\overline{x}\right)^2$	
1	80	80-80=0	0		80	80-80=0	0	
2	81	81-80=1	1		70	70-80=-10	100	
3	79	79-80=-1	1		90	90-80=10	100	
4	82	82-80=2	4		85	85-80=5	25	
5	78	78-80=-2	4		75	75-80=-5	25	
6	79	79-80=-1	1		82	82-80=2	4	
7	81	81-80=1	1		78	78-80=-2	4	
Sum	560		12/6 = 2	$= S_1^2$	560		258/6 = 43	$= S_2^2$
avg (mean)	$\overline{x}_1 = \frac{560}{7} = 80$		(Vari	ance)	$\overline{x_2} = \frac{560}{7} = 80$		(Varia	nce)
Standar	d Deviation =	= $\sqrt{(S_1)^2}$	= 1.4			$\sqrt{(S_2)^2}$		

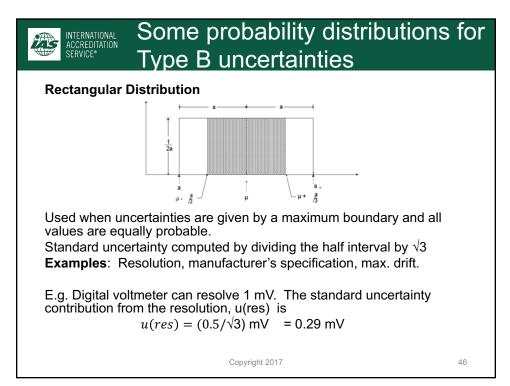
C	loulatin	a the M	lean ar	d Sta	ndard De	viation	of a Sam	nlo
		Data S			ndard Deviation of a Sample Data Set 2			
Point No.	<i>x</i> <sub>1</sub>	$\left(x-\overline{x}\right)$	$\left(x-\overline{x}\right)^2$		<i>X</i> <sub>2</sub>	$\left(x-\overline{x}\right)$	$\left(x-\overline{x}\right)^2$	
1	80	80-80=0	0		80	80-80=0	0	
2	81	81-80=1	1		70	70-80=-10	100	
3	79	79-80=-1	1		90	90-80=10	100	
4	82	82-80=2	4		85	85-80=5	25	
5	78	78-80=-2	4		75	75-80=-5	25	
6	79	79-80=-1	1		82	82-80=2	4	
7	81	81-80=1	1		78	78-80=-2	4	
Sum	560		12/6 = 2	$= S_1^2$	560		258/6 = 43	$= S_2^2$
avg (mean)	$\overline{x_1} = \frac{560}{7} = 80$		(Vari	ance)	$\overline{x_2} = \frac{560}{7} = 80$		(Varia	nce)
Standar	Deviation =	$= \sqrt{(S)^2}$	= 1.4			$\sqrt{(S_2)^2}$	= 6,557	

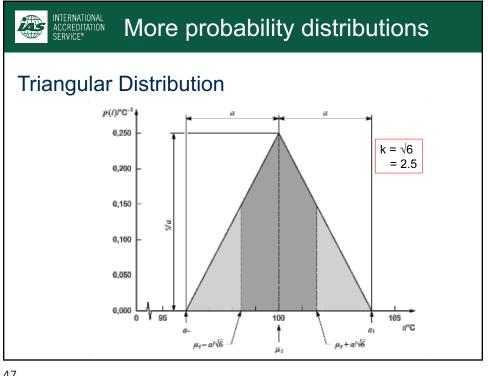


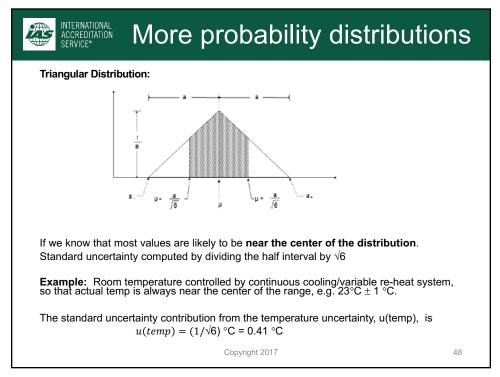


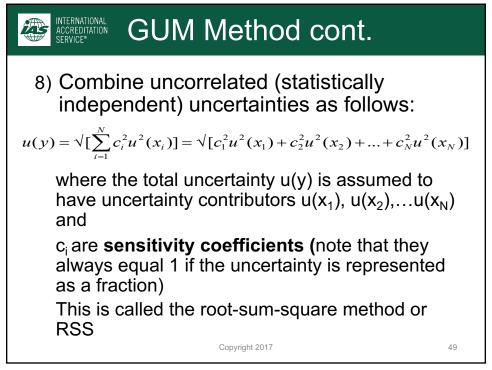


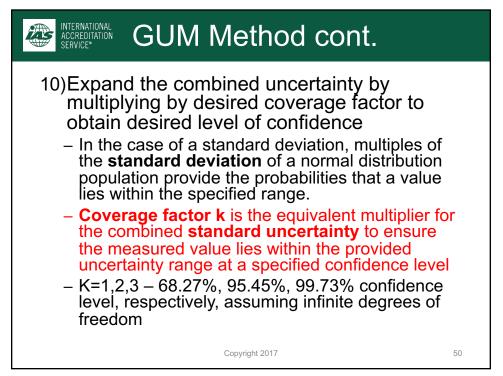


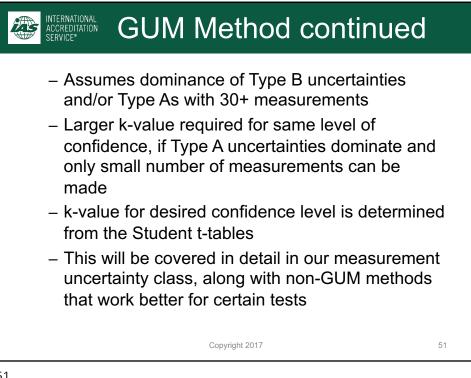


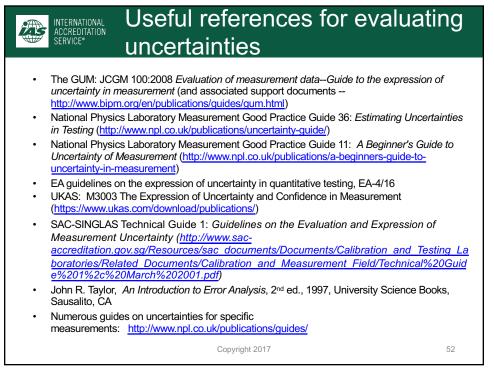


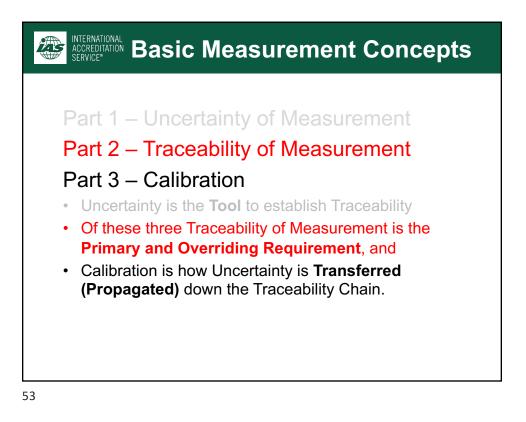


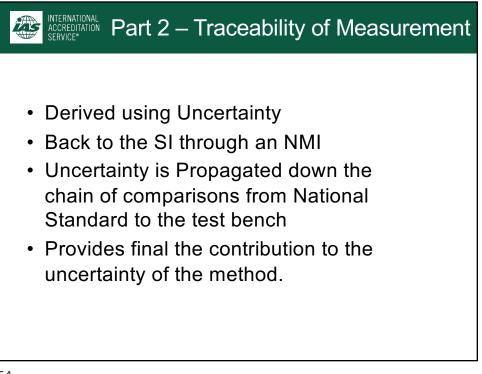


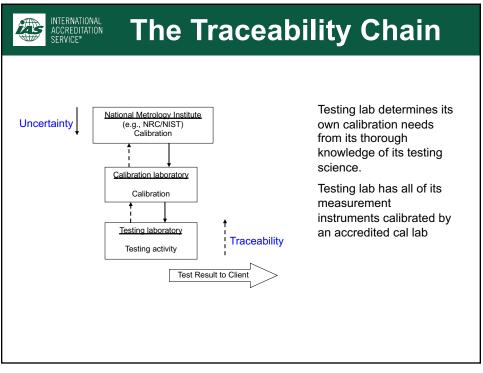


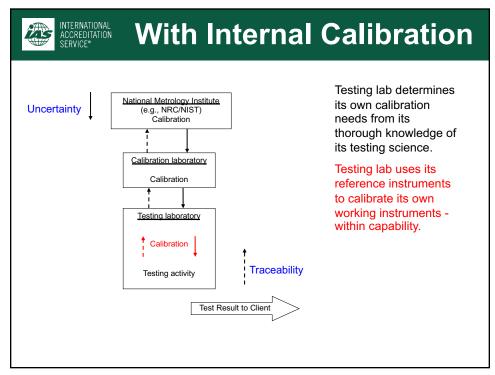


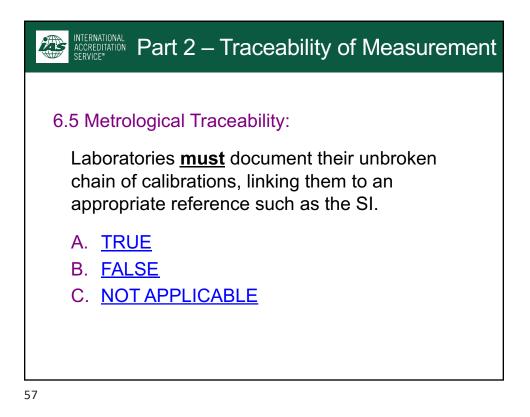


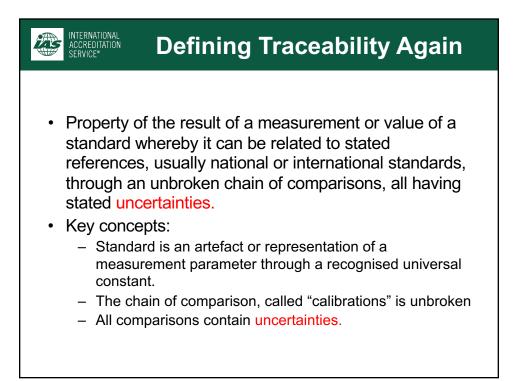


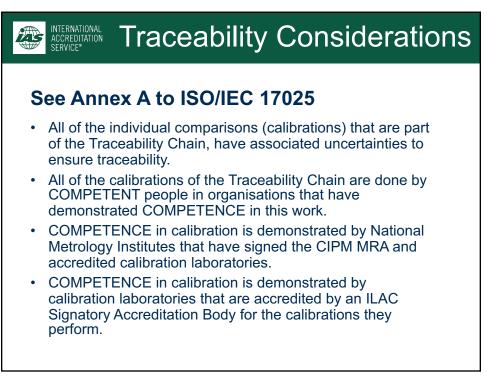


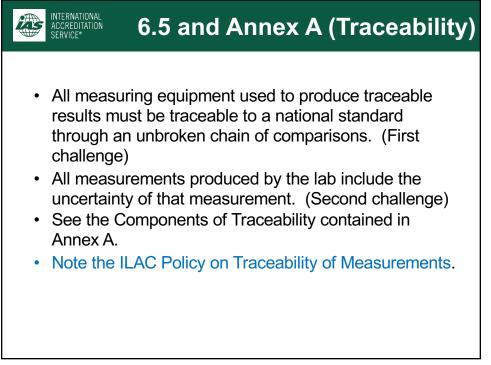


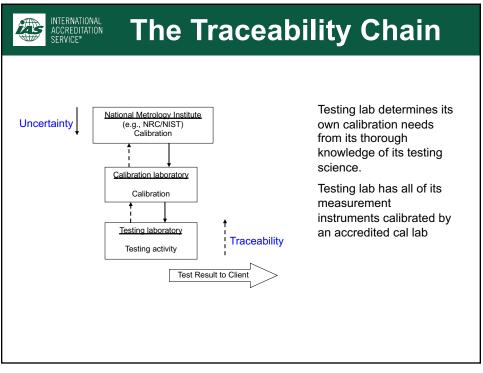


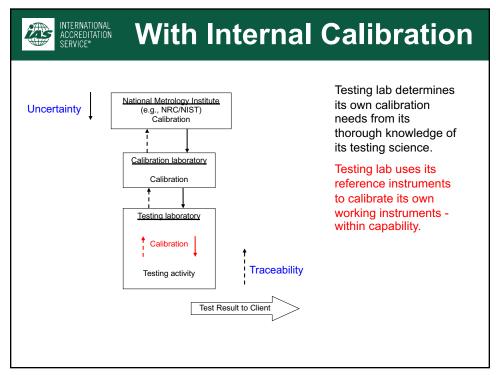


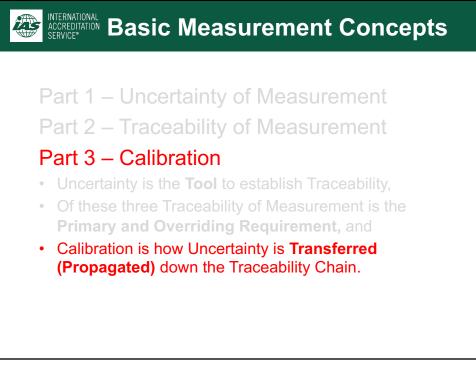


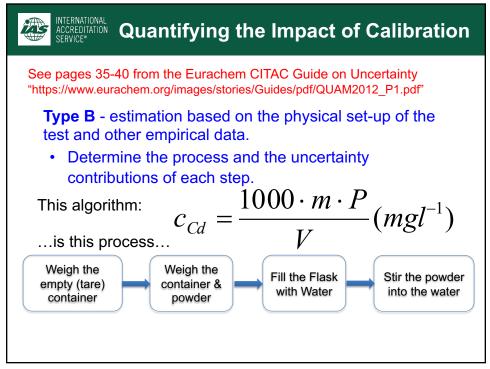


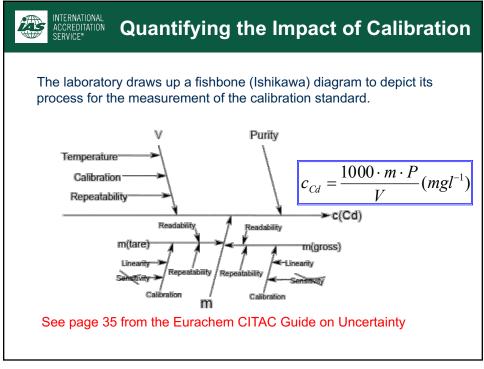








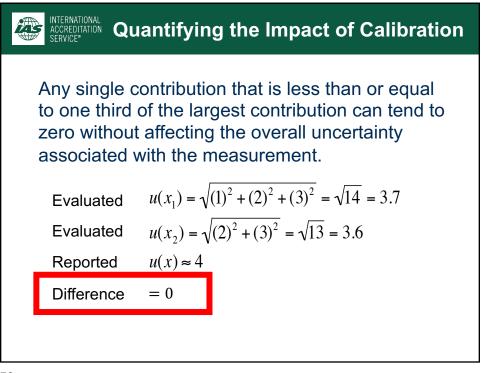


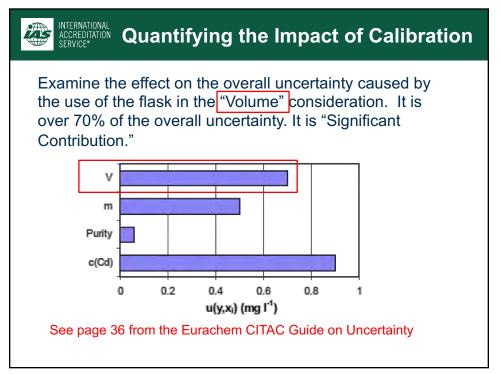


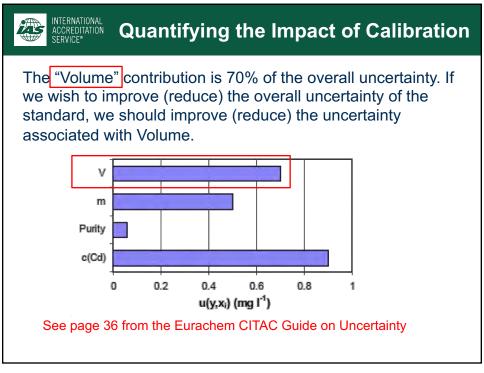
ulatin	a the M		d Sta	ndard Do	viation	of a Sam	nlo
ulating	and the second s		iu sta	Data Set 2			
<i>x</i> <sub>1</sub>	$\left(x-\overline{x}\right)$	$\left(x-\overline{x}\right)^2$		<i>X</i> <sub>2</sub>	$\left(x-\overline{x}\right)$	$\left(x-\overline{x}\right)^2$	
80	80-80=0	0		80	80-80=0	0	
81	81-80=1	1		70	70-80=-10	100	
79	79-80=-1	1		90	90-80=10	100	
82	82-80=2	4		85	85-80=5	25	
78	78-80=-2	4		75	75-80=-5	25	
79	79-80=-1	1		82	82-80=2	4	
81	81-80=1	1		78	78-80=-2	4	
560		12/6 = 2	$= S_1^2$	560		258/6 = 43	$= S_2^2$
$=\frac{560}{=80}$			1	$\frac{1}{x_1} = \frac{560}{1} = 80$		(Varia	
7				7			
eviation =	= $\sqrt{(S_1)^2}$	= 1.4			$\sqrt{(S_2)^2}$	= 6.557	
				Standard D	Deviation of	the mean =	
	$x_1$ 80 81 79 82 78 79 81 560 $=\frac{560}{7}=80$ eviation =	$\begin{array}{c c} \textbf{Data S} \\ x_i & \left(x - \overline{x}\right) \\ 80 & 80 - 80 = 0 \\ 81 & 81 - 80 = 1 \\ 79 & 79 - 80 = -1 \\ 82 & 82 - 80 = 2 \\ 78 & 78 - 80 = -2 \\ 78 & 78 - 80 = -2 \\ 79 & 79 - 80 = -1 \\ 81 & 81 - 80 = 1 \\ \hline 560 \\ \hline \hline \\ \textbf{eviation} = \sqrt{\left(S_i\right)^2} \end{array}$	Data Set 1 $x_i$ $\left(x - \overline{x}\right)$ $\left(x - \overline{x}\right)^2$ 8080-80=008181-80=117979-80=-118282-80=247878-80=-247979-80=-118181-80=1156012/6 = 2	Data Set 1 $x_i$ $\left(x - \overline{x}\right)$ $\left(x - \overline{x}\right)^2$ 80         80-80=0         0           81         81-80=1         1           79         79-80=-1         1           82         82-80=2         4           78         78-80=-2         4           79         79-80=-1         1           81         81-80=1         1           560         12/6 = 2 = S_1^2 $= \frac{560}{7} = 80$ (Variance)           eviation = $\sqrt{(S_1)^2}$ = 1.4	Data Set 1 $x_1$ $(x - \overline{x})$ $(x - \overline{x})^2$ $x_2$ 80         80-80=0         0         80           81         81-80=1         1         70           79         79-80=-1         1         90           82         82-80=2         4         85           78         78-80=-2         4         75           79         79-80=-1         1         82           81         81-80=1         1         78           560         12/6 = 2 = S_1^2         560 $\overline{560}$ $\overline{7}$ 80           eviation = $\sqrt{(S_1)^2}$ = 1.4 $\overline{7}$	Data Set 1Data $x_1$ $(x - \overline{x})$ $(x - \overline{x})^2$ $x_2$ $(x - \overline{x})$ 8080-80=008080-80=08181-80=117070-80=-107979-80=-119090-80=108282-80=248585-80=57878-80=-247575-80=-57979-80=-118282-80=28181-80=117878-80=-256012/6 = 2 = S_1^2560 $\overline{x_2} = \frac{560}{7} = 80$ eviation = $\sqrt{(S_1)^2}$ = 1.4 $\sqrt{(S_2)^2}$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$

**EXAMPLE** Quantifying the Impact of Calibration  
• Using Type B uncertainty estimations, they would  
arrive at a result similar to the one from Type A.  
• This algorithm: 
$$c_{Cd} = \frac{1000 \cdot m \cdot P}{V} (mgl^{-1})$$
  
would produce this uncertainty expression:  
 $u_c(c_{Cd}) = c_{Cd} \sqrt{\left(\frac{u(P)}{P}\right)^2 + \left(\frac{u(m)}{m}\right)^2 + \left(\frac{u(V)}{V}\right)^2}$   
See page 35 from the Eurachem CITAC Guide on Uncertainty

		• • •	pe B	
	Description	Value	Standard uncertainty	Relative standard uncertainty u(x)/x
P	Purity of the metal	0.9999	Type B 0.000058	0.000058
m	Mass of the metal	100.28 mg	Type B 0.05 mg	0.0005
V	Volume of the flask	100.0 ml	Type B 0.07 ml	0.0007
c <sub>ca</sub>	concentration of the calibration standard	$1002.7 \text{ mg } \mathrm{I}^{-1}$	0.9 mg 1 <sup>-1</sup>	0.0009 Type B







ias

## INTERNATIONAL ACCREDITATION SERVICE\* Quantifying the Impact of Calibration

"Volume" standard uncertainty is the result of flask tolerance statement (not calibration as stated in the example), repeatability, and temperature considerations:

$$u(V) = \sqrt{u(cal)^{2} + u(repeatability)^{2} + u(temperature)^{2}}$$

The flask is not calibrated. The manufacturer "derives" calibration from "tolerance." This is the expression used.

$$u(V) = \sqrt{(0.04)^2 + (0.02)^2 + (0.05)^2} = 0.07ml$$

See page 38 from the Eurachem CITAC Guide on Uncertainty

